

Semester Two Examination, 2021

Question/Answer booklet

MATHEMATICS SPECIALIST UNITS 1&2			If required by your examination administrator, please place your student identification label in this box					
Section One: Calculator-free								
WA student number:	In figures							
	In words							
	Your nam	ie						
Time allowed for this a Reading time before commen		five mir			ar		of additic ooklets ι ible):	

fifty minutes

Materials required/recommended for this section

To be provided by the supervisor This Question/Answer booklet Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Working time:

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	50	35
Section Two: Calculator-assumed	13	13	100	92	65
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Instructions to candidates

- 1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen. Do not use erasable or gel pens.
- 3. You must be careful to confine your answers to the specific question asked and to follow any instructions that are specific to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams.
- 6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Markers use only				
Question	Maximum	Mark		
1	6			
2	5			
3	6			
4	6			
5	6			
6	7			
7	6			
8	8			
S1 Total	50			
S1 Wt (×0.7)	35%			
S2 Wt	65%			
Total	100%			

SPECIALIST UNITS 1&2

Section One: Calculator-free

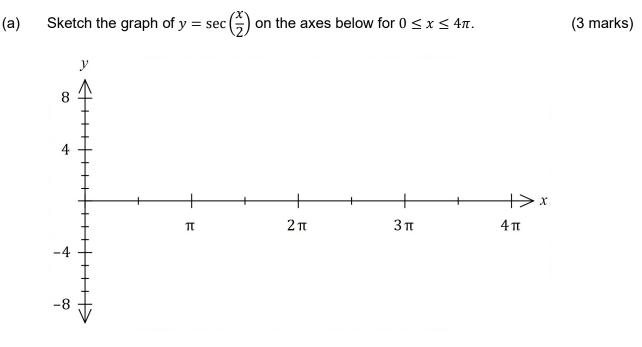
This section has **eight** questions. Answer **all** questions. Write your answers in the spaces provided.

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Working time: 50 minutes.

Question 1

(6 marks)



(b) Prove the identity $\csc 2A - \cot 2A = \tan A$.

(3 marks)

Question 2 (5 r				
Let matrix $A = \begin{bmatrix} 2 & 3 \\ -1 & 0 \end{bmatrix}$ and matrix $B = \begin{bmatrix} 2k+1 & 3 \\ 1 & k-2 \end{bmatrix}$, where k is a constant.				
(a) When $k = 2$, determine				
(i) AB .	(1 mark)			

(ii) 2A - 3B. (2 marks)

(b) Determine the value(s) of k if matrix **B** is singular. (2 marks)

See next page

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CALC	CULATOR-FREE	5	SPECIALIST UNITS 1&2
	tion 3		(6 marks)
	$z = \sqrt{5} + 3i$ and $z_2 = \sqrt{5} - i$. Determine exists $2z_1 - z_2$.	ach of the following in th	ne form <i>a</i> + <i>bi</i> . (1 mark)
(b)	$iar{z}_1.$		(1 mark)
(c)	$z_1 \times z_2$.		(2 marks)
(d)	$Z_1 \div Z_2.$		(2 marks)

See next page

SPECIALIST UNITS 1&2 6		CALCULATOR-FREE		
Ques	stion 4			(6 marks)
(a)	Determine the value(s) of the constant a	t given that $\begin{bmatrix} -2\\t \end{bmatrix}$		(2 marks)

(b) Determine A^{-1} when $A = \begin{bmatrix} 7 & 3 \\ -2 & 2 \end{bmatrix}$. (2 marks)

(c) Show use of matrix methods to solve the following system of linear equations:

7x + 3y - 25 = 02y - 2x + 10 = 0

(2 marks)

CAL	CULATOR-FREE	7	SPECIALIST UNITS 1&2
Ques	stion 5		(6 marks)
(a)	Using a product identity, or otherwise,	evaluate $\cos\left(\frac{\pi}{12}\right) - \cos\left(\frac{\pi}{12}\right)$	$s\left(\frac{5\pi}{12}\right)$. (3 marks)

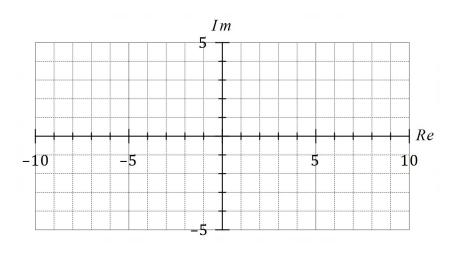
(b) Solve the equation $2\cos^2 2x = 3\sin 2x$, $0 \le x \le 2\pi$.

(3 marks)

Question 6 (7 marks) Determine all complex solutions to the equation $z^2 - 10z + 27 = 0$. (a)

 $z_1 = -4 - i$ is a solution to f(z) = 0, where f(z) is a real quadratic polynomial. (b)

- State z_2 , another solution to f(z) = 0. (i)
- Let $z_3 = z_2 z_1$. Plot and label z_1, z_2 and z_3 in the complex plane below. (2 marks) (ii)



Determine f(z), given that the coefficient of its z^2 term is 1. (iii) (2 marks)

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(2 marks)

(1 mark)

Question 7

(6 marks)

Use mathematical induction to prove that $2^{5n} - 5^n$ is divisible by 9 for all integers $n \ge 1$.

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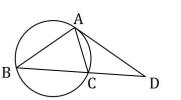
Question 8

(b)

(a) Points *A*, *B* and *C* lie on a circle.

The tangent to the circle at A intersects secant BC at point D.

Prove that $AD^2 = BD \times CD$.



(8 marks)

Two unequal circles intersect at P and Q. A common tangent touches one circle at R and the other circle at S. PQ produced intersects RS at X. Prove that X bisects RS. (4 marks)

Question number: _____

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